

**Advanced  
Complete**  
**MathSmart<sup>®</sup>**

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***Basic Problem-solving Questions***

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# 6

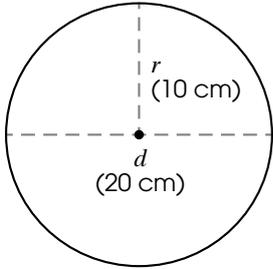
## Circles

solving a variety of word problems that involve properties of circles, such as radius, diameter, circumference, and area



### Math Skills

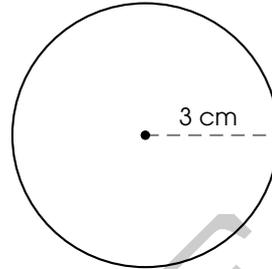
①



radius ( $r$ )  
 cm

diameter ( $d$ )  
 cm

②



$r =$  \_\_\_\_\_

$d =$  \_\_\_\_\_

**Circumference ( $C$ ) =  $2\pi r$  or  $\pi d$**

$$2\pi r$$

$$= 2 \times 3.14 \times \text{[ ]}$$

$$= \text{[ ]} \text{ (cm)}$$

$C =$

**Area ( $A$ ) =  $\pi r^2$**

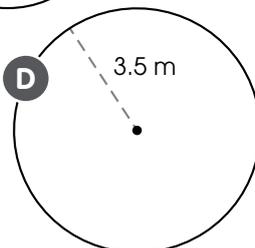
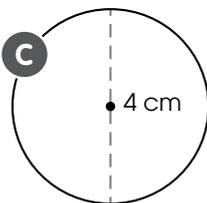
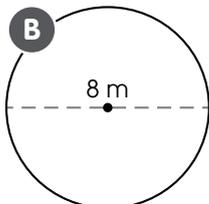
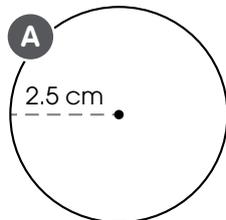
$$\pi r^2$$

$$= 3.14 \times \text{[ ]}^2$$

$$= \text{[ ]} \text{ (cm}^2\text{)}$$

$A =$

③



**Circumference**

**Area**

	Circumference	Area
A	_____ cm	_____ cm <sup>2</sup>
B	_____	_____
C	_____	_____
D	_____	_____

- ⑦ A round mirror has an area of  $0.1 \text{ m}^2$ . What is the diameter of the mirror in centimetres?



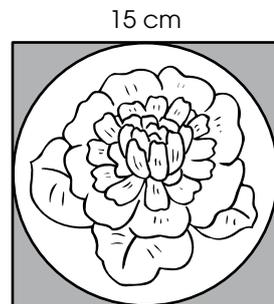
**Hints**

$1 \text{ m}^2 = 10\,000 \text{ cm}^2$

- ⑧ A Canadian toonie is made up of an inner circle with an outer ring. What is the area of the outer ring?



- ⑨ A tile design has a circle inside a square. What is the total area of the shaded parts?



- ⑩ Josephine measured her finger for a ring. She wrapped tape measure around her finger and measured 57 mm. What would the size of her ring be?

Ring Size	Diameter (mm)
7	17.3
8	18.2
9	19.0
10	19.8

- ① Company A sells a \$1029 phone at 15% off, while Company B sells the phone for \$34.25 cheaper than the discounted price of Company A after a 12% discount. How much did Company B sell the phone for originally?

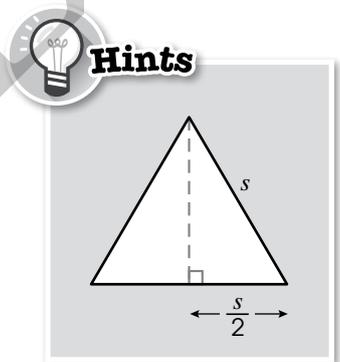
Discounted price at Company A: \_\_\_\_\_  $\times$  (1 - \_\_\_\_\_) = \_\_\_\_\_

Discounted price at Company B: \_\_\_\_\_ - \_\_\_\_\_ = \_\_\_\_\_

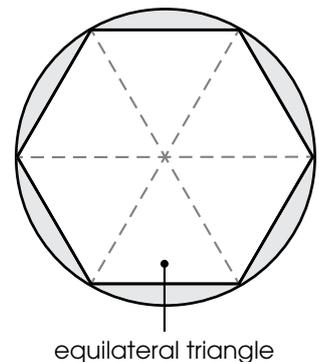
Original price at Company B: \_\_\_\_\_  $\div$  (1 - \_\_\_\_\_) = \_\_\_\_\_

Company B sold the phone for \_\_\_\_\_ originally.

- ② Find a polynomial that describes the area of an equilateral triangle with a side length of  $s$ . Keep the numbers as square roots.



- ③ A coaster has a regular hexagon where each vertex lies on the edge of the circle as shown. If the coaster has a diameter of 8 cm, what is the area of the shaded part?



**Topics covered:**

**Question 1**

- decimals
- percents

**Question 2**

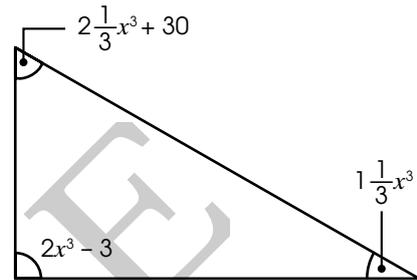
- Pythagorean relationship
- polynomials

**Question 3**

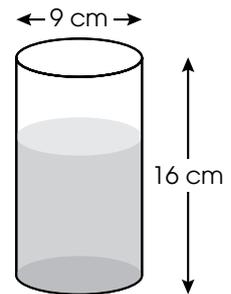
- circles
- Pythagorean relationship

- ④ In a studio audience of 400 people, 85.75% are adults. If 2 members of the audience are picked at random, what is the probability that they are both children?

- ⑤ What is the value of  $x$ ?



- ⑥ How much water in millimetres can be added if the cylindrical glass is  $\frac{2}{3}$  full?



- ⑦ A spherical sponge has a diameter of 10 cm. When soaked, its surface area increases by 44%. What is the diameter of the sponge when soaked?

**Topics covered:**

**Question 4**

- percents
- probability

**Question 5**

- angles
- equations

**Question 6**

- fractions
- volume

**Question 7**

- percents
- surface area
- equations